

1. $a = k/b$; $4 = k/6$; $k = 24$; $a = 24/-12$; $a = -2$

b. -2

2. $\begin{vmatrix} 5 & 6 \\ 7 & 8 \end{vmatrix} = 5 \times 8 - 7 \times 6 = 40 - 42 = -2$

a. -2

3. $x = \frac{4}{7}$ is a vertical line. No slope.

e. NOTA

4. Center (3, -2) and horiz radius 5 implies 2 y-int's. Vert radius 3 implies 2 x-int's.

d. 4

5. ${}_6C_3 \times {}_7C_2 = 20 \times 21$

b. 420

6. $-19 = a_1 + 12d$ and $10 = a_1 + 4d$. $-29 = 8d$. $d = -29/8$. $a_1 = 10 - 4(-29/8) = 80/8 + 116/8 = 196/8$.

$a_2 = 196/8 + -29/8 = 167/8$.

b. $\frac{167}{8}$

7. $f(2) = 1/3$. $f(1/3) = 3/4$. $f(3/4) = 4/7$. $f(4/7) = 7/11$

b. $\frac{7}{11}$

8. $y = \frac{3x+5}{7-|x|}$. As x approaches infinity, y approaches -3. As x approaches negative infinity, y

approaches 3. Vertical asymptotes at $x = 7$ and $x = -7$.

c. 4

9. $y = \frac{250}{1+3e^{-.05x}}$. As x approaches infinity, $e^{-.05x}$ approaches zero and y approaches 250.

d. 250

10. Slope $(-2, 1)$ and $(1, -3) = 4/-3$. Slope of tangent line is perpendicular to slope of the attached radius = $3/4$.

c. $\frac{3}{4}$

11. Build x, f, g table.

x =	5	4	3	2	1	0	-1	-2
f =	625	256	81	16	1	<u>0</u>	<u>1</u>	16
g =	1024	256	64	16	4	<u>1</u>	<u>0.25</u>	0.0625

Since $f > g$ at $x = -1$ and $f < g$ at $x = 0$, there must be a third point of intersection/solution.

d. 3

12. Divide both sides by 5 and split the absolute value: $-3 \leq x - 7 \leq 3$. Add 7. $4 \leq x \leq 10$.

d. $[4, 10]$

13. $l \times w \times h = 50$. $l = 2w$. $h = 25/w^2$. $S = lw + 2wh + 2hl = 2ww + 2w(25/w^2) + 2(2w)(25/w^2)$

$$S = 2w^2 + 50/w + 100/w.$$

c. $S(x) = 2x^2 + \frac{150}{x}$

14. $y = 2(x-3)^2 - 7$. 0 for x. $y = 2(0-3)^2 - 7 = 2(9) - 7 = 18 - 7 = 11$.

e. **NOTA**

15. $a \times b/2 = 120$. $ab = 240$. $a + b + \sqrt{a^2 + b^2} = 60$. $a + b + \sqrt{a^2 + b^2} = 60$.

$$a + b - 60 = -\sqrt{a^2 + b^2}. (a + b - 60)^2 = a^2 + b^2 = a^2 + ab - 60a + ba + b^2 - 60b - 60a - 60b + 3600.$$

$$120a + 120b = 3600 + 2ab = 3600 + 2(240). a + b = 30 + 4$$

b. 34

16. $10x^5 + 6x^4 - 49x^3 + 33x^2 - 96x + 36 = 0$. Possible rat. roots: $\frac{\pm 1, 2, 3, 4, 6, 9, 12, 18, 36}{1, 2, 5, 10}$

Synthetic substitution:

	10	6	-49	33	-96	36
$x = 2/5 \mid$	10	10	-45	15	-90	0

reduce the polynomial:

	2	2	-9	3	-18
$x = 2 \mid$	2	6	3	9	0

$2x^3 + 6x^2 + 3x + 9$ factor by grouping: $(2x^2 + 3)(x + 3)$. Non-real and negative solutions. $2 + 2/5 =$

c. $\frac{12}{5}$

17. $y = -\sqrt{x+5} - 6$. Domain: $[-5, \infty)$. Range: $(-\infty, -6]$. No intersection.

e. **NOTA**

18. If $z = a + bi$, then $z \cdot \bar{z} = (a + bi)(a - bi) = a^2 - abi + abi - b^2i^2 = a^2 - b^2(-1)$

a. $a^2 + b^2$

19. $\frac{1}{5}$ = probability of guessing right, for 20 questions $\left(\frac{1}{5}\right)^{20}$. $\frac{4}{5}$ probability of guessing wrong, for

10 questions $\left(\frac{4}{5}\right)^{10}$. ${}_{30}C_{20}$ possible arrangements of 20 questions from 30 total.

d. ${}_{30}C_{20} \left(\frac{1}{5}\right)^{20} \left(\frac{4}{5}\right)^{10}$

20. $A \times B = B \times A$ is generally false. True for inverses or identity matrix.

b. **sometimes**

21. $f(x) = 3x + 7$. By definition, switch x and y. Solve for y.

b. $\frac{x-7}{3}$

22. y-intercept of $y = 4x^5 + 9x^4 - 2x^2 - 3x$

a. $(0, 0)$

23. $15D + 1C + .25M = 100$. $D + C + M = 100$. Subtract the two: $14D - 3/4 M = 0$. $14D = 3/4 M$. $14 \cdot 4D = 3M$. D must be a positive multiple of 3 (3, 6, 9, ...). $D = 9$ exceeds the \$100. $D = 6$ costs \$90, but does not leave enough \$ for 94 other animals. So $D = 3$ and $M = 56$ and $C = 41$.

a. 1

24. By definition, $f(a) = f(-a)$. So, I (yes), II (not a function), III (yes), IV (no).

d. I, III

25. $y = (x-4)(x+2)$. X-intercepts (4, 0) and (-2, 0). Vertex is half way between: $(4 + -2)/2 = 1$.

Substitute: $y = (1 - 4)(1 + 2) = -9$. $1 + -9 = -8$

b. -8

26. $\sqrt{3-x} + \sqrt{x+2} = 3 = 2+1 = 1+2$. $3-x = 4$. $x = -1$. $3-x = 1$. $x = 2$. $-1 + 2 = 1$.

b. 1

27. $\frac{(x-h)^2}{A} + \frac{(y-k)^2}{B} = 1$. Cannot be determined since focus location based on ellipse's orientation.

d. cannot be determined

28. $C + G = 44$ and $2C + 4G = 156$. Simplify: $C + 2G = 78$. Subtract: $G = 34$

c. 34

29. $\sum_{n=1}^{\infty} 5 \left(\frac{1}{2}\right)^{n-1} = 5 + \frac{5}{2} + \frac{5}{4} + \frac{5}{8} + \frac{5}{16} + \dots = 5 \left(1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots\right) = 5(2)$

b. 10

30. $\log_6(\log_2 x) = 1$. $(\log_2 x) = 6$. $x = 2^6 = 64$.

b. 4