

1.  $f(x) = x^2 - 10x + 25$

Let  $A$  be the discriminant of  $f$ .

Let  $B$  be the coefficient of the  $x$  term of the expansion of  $f(x-4)$ .

Let  $C$  be the largest root of the resulting function if the graph of  $f$  is lowered 1 unit.

Let  $D$  be the  $y$ -intercept of the new function if the graph of  $f$  is translated to the right 1 unit.

Give the value of  $A + \frac{D}{B+C}$ .

2.  $S = \{ 1, 2, 4, 5 \}$  and  $T = \{ 3, 6, 9, 12 \}$ .

**Let  $A$**  be the probability that an element is randomly chosen from each of sets  $S$  and  $T$ , and the two numbers have a sum of less than 5.

**Let  $B$**  be the probability that an element is randomly chosen from each of sets  $S$  and  $T$ , and both are prime.

**Let  $C$**  be the probability that 2 distinct elements are randomly chosen from set  $S$ , without replacement, and both are even.

Find the value of  $\frac{B \cdot C}{A}$ .

3. A right circular cylindrical container has radius 6 feet, and height 20 feet. It is filled to  $\frac{1}{4}$  of its height with water.

**Let  $A$**  be the amount of water, in cubic feet, which will have to be added to the container in order to raise the water level 1 foot.

**Let  $B$**  be the height in feet of water, if the volume of water is increased by 10%.

**Let  $C$**  be the height in feet of water if the original radius was decreased by 20%, and the amount of water remained the same.

A speck of dust is floating on the top surface of the water in the container. **Let  $D$**  be the maximum distance in feet between the speck and a point on the bottom base's circumference.

Give the value of  $\frac{A}{\pi} + 10B + 32C + D$ .

4. In a company, there were exactly 40 employees on January 1, 2009. Of those employees, 20 each made \$10 per hour, and the rest each made \$5 per hour. On February 1, 2009, ten (10) of these employees quit their job at this company.

Let  $A$  be the least possible average (arithmetic mean) per hour pay at this company on February 2, 2009, if no other employees quit and no new employees were hired.  $A$  should be written as a fraction in reduced form.

Let  $B$  be the least possible number of employees who can be hired on February 2, 2009 at \$10 per hour to make sure that the average (arithmetic mean) per hour pay is greater than \$9, if the quitters had all made \$5 per hour.

Give the value of  $6A + B$ .

5. Let  $A$  be the least positive value of  $x$  such that  $|2x - 10| = 9$ .

Let  $B$  be the least integral value of  $x$  such that  $|3 - 4x| < 10$ .

Let  $C$  be the positive value of  $x$  such that  $\frac{x+1}{4x^2} - \frac{x+3}{2x} = \frac{-3}{8x}$ .

Let  $D$  be the value of  $x$  such that  $\sqrt{x+1} = \sqrt{x+3}$ .

Give the value of  $A + B + C + D$

6. I.  $u + v$       II.  $u + 1$       III.  $|1 - u|$       IV.  $2uv$

Let  $A$  be the number of values above (I through IV) which must be odd for  $u$  and  $v$  both odd.

Let  $B$  be the number of values above (I through IV) which must be even if  $u$  and  $v$  are both even.

Let  $C$  be the number of values above (I through IV) which must be odd for  $u$  an odd integer and  $v$  an even integer.

Let  $D$  be the number of values above (I through IV) which must be even for  $u$  an odd integer and  $v$  an even integer.

Find the sum  $A + B + C + D$ .

7. Let  $R$ ,  $S$  and  $T$  be three consecutive odd integers, respectively.

If  $R + T = 34$  then let  $A$  be the value of  $R + S + T$ .

If  $T$  is 5 times  $R$  then let  $B = 3S$ .

If  $S + T = 44$  then let  $C = R + S$ .

Let  $D$  be the value of  $\frac{R - T}{R - S}$ .

Give the value of  $A + B + C + D$ .

8.  $R^{\frac{1}{3}} \square R^{\frac{1}{3}} \square R^{\frac{1}{3}} = 8$       and       $S^{\frac{2}{3}} \square S^{\frac{2}{3}} \square S^{\frac{2}{3}} = 8$

Let  $A = \sqrt{R^{\frac{2}{3}}}$ .

Let  $B$  be the largest possible value of  $S^2 - S$ .

Let  $C$  be the smallest possible value of  $\frac{7}{1+S}$ .

Give the value of  $A + B + C$ .

9.  $x^2 + y^2 - 2x + 4y - 4 = 0$

Let  $A\pi$  be the area of the conic represented by the equation above.

Let  $B$  be the number of intersection points with the graph of the conic and the line  $y = 0.5$ .

Let  $C$  be the distance between the center of the conic and the point  $(7, 6)$ .

Give the value of  $A + B + C$ .

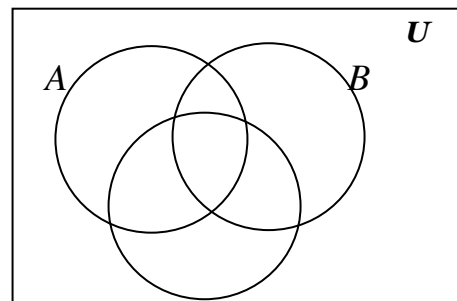
10. Sets  $A$ ,  $B$  and  $C$  have 20, 30 and 10 elements respectively.

$A \cap B$  has 4 elements.  $A \cap C$  has 5 elements.

$B \cap C$  has 2 elements.  $A \cap B \cap C$  has 1 element.

Let  $R$  be the number of elements in set  $A \cup B \cup C$ .

Let  $S$  be the number of elements in set  $A$  but not in set  $B$ .



Give the value of  $R + S$ .

11. Let  $x = 2 + 3i$ ,  $y = 1 - i$  and  $z = 1 + i$ .

Let  $A = \frac{y}{z}$  and

let  $B = x \square y$  and

let  $C = |x + y + z|$  and

let  $D = y^2 + z^2$ .

Give the value of  $A + B + C + D$ .

12. Let  $A$  be the solution of  $3x^{\frac{3}{2}} + 4 = 28$ .  
Let  $B$  be the real solution of  $3x - 11\sqrt{x} = 4$ .

Give the value of  $A+B$ .

13. Consider graph  $G_1$  with equation  $4(y-1)^2 - 9(x+2)^2 = 36$  and  
graph  $G_2$  with equation  $4(x-1)^2 + (y+2)^2 = 16$ .

Let  $A$  be the absolute value of the slope of an asymptote of  $G_1$ .

Let  $B$  be the length of the major axis of  $G_2$ .

Let  $C$  be the greatest y-intercept of any asymptote of  $G_1$ .

Let  $(D, E)$  and  $(F, H)$  be the coordinates of the foci of  $G_2$  for  $E < H$ .

Give the sum  $36A + B + C + D + H$ .

14. If  $x^2 = 4$  and  $y^2 = 25$  and  $z^2 = 1$  then

let  $A$  be the least possible value of  $|x + y - z|$  and

let  $B$  be the greatest possible value of  $|x + y - z|$ .

Give the value of the product  $A \square B$ .