

**February Regional****Algebra II Team Question 1**

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Consider the following numbers:  $-5, 0, 2, -\frac{1}{2}, -3, \frac{7}{8}, 14, -\frac{8}{3}, 2.43, 7\frac{1}{2}$

Let A be equal to the product of the natural numbers.

Let B be equal to the sum of the whole numbers.

Of the ten numbers listed, let C be equal to how many of them are rational.

Let D be equal to the sum of the integers.

Find  $\frac{AC}{BD}$ .

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For a linear function  $f$ ,  $f(-1)=3$  and  $f(2)=4$ . The domain of function,  $f$ , is all real numbers.

Let A be equal to  $f(3)$ .

Let B be equal to  $a$  such that  $f(a)=10$ .

Let C be equal to the y-intercept of  $f(x)$ .

Let D be equal to  $b$  such that  $f^{-1}(b)=5$ .

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Find the area of the triangle defined by the solution to the system of inequalities:

$$\begin{cases} x - y \leq 2 \\ x + 2y \geq 8 \\ y \leq 4 \end{cases}$$

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If  $f(x) = x^2 + 6x + 7$ , the coordinates of the vertex,  $(h, k)$ , and the roots are  $A$  and  $B$ , find  $\frac{h \cdot k}{A + B}$ .

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Let A be equal to  $\sqrt{2+\sqrt{2+\sqrt{2+\dots}}}$  .

Let B be equal to  $\sqrt{2-\sqrt{2-\sqrt{2-\dots}}}$  .

Find  $2A+3B$  .

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Find  $2A+3B$  .

Let A be equal to the number of unique possible rational values that could be zeros of  $f(x) = x^3 + kx^2 + 5x + 4$  for  $k$ , an integer.

Let B be equal to the number of positive real zeros of  $f(x) = x^3 + 2x^2 + 5x + 4$ .

Let C be equal to the number of complex zeros of the polynomial equation  $x^3 + 2x^2 + 5x + 4 = 0$ .

Let D be equal to the sum of the coefficients of  $g(x)$ , given that  $g$  has integral coefficients, has the smallest degree, and has roots 2 and  $2 + i$ .

Find the mean of A, B, C, and D.

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Find the mean of A, B, C, and D.

**February Regional****Algebra II Team Question 7**

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Let A equal the coefficient of the seventh term of the expansion of  $(x - 2y)^6$ .

Let B equal the coefficient of the fourth term of the expansion of  $(x + 1)^8$ .

Let C equal the coefficient of the first term of the expansion of  $(2x + 3y)^4$ .

Find  $\frac{A+B}{C}$ .

**February Regional****Algebra II Team Question 7**

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Let C equal the coefficient of the first term of the expansion of  $(2x + 3y)^4$ .

Find  $\frac{A+B}{C}$ .

Let A be equal to the smallest solution of  $3^{x^2+4x} = \frac{1}{27}$

Let B be equal to the largest solution of  $3^{5x} \cdot 9^{x^2} = 27$ .

Let C be equal to the sum of the real solutions of  $\log_4(x+3) + \log_4(x-3) = 2$ .

Find A+B+C.

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Let A be equal to  $i^{122}$ .

Let B be equal to  $\frac{3+i}{2-i}$

Let C be equal to  $-i\sqrt{-144}$

Let D be equal to  $(4+i)^2$

Find  $A+B+C+D$  and write in simplified form.

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Given  $f(x) = \frac{x^2 + 6x + 5}{x^2 + 5x + 4}$ ,

Let A be equal to the sum of all possible values of  $r$  for which  $y = r$  is an asymptote of  $f$ .

Let B be equal to the sum of all possible values of  $p$  for which  $x = p$  is an asymptote of  $f$ .

Let C be equal to the y-coordinate of the removable discontinuity.

Find  $\frac{AC}{B}$ .

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**February Regional****Algebra II Team Question 11**

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Given that  $x = \log 3$  and  $y = \log 5$ , then let

A = the value of  $\log 500$  in terms of  $x$  and/or  $y$ .

B = the value of  $k$  that makes  $2x + 3y = \log(9k)$  true.

C = the value of  $\frac{\log_2 5}{\log_2 10}$  in terms of  $x$  and/or  $y$ .

Give a simplified expression for  $(A + B) - C$ .

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Give a simplified expression for  $(A + B) - C$ .

Let A be the harmonic mean of 2, 4, 5, and 10.

Let B be the arithmetic mean of 2, 4, 5, and 10.

Let C be the geometric mean of 1, 3, and 9.

Find the product of A, B, and C.

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Find the product of A, B, and C.

Solve for x:  $\frac{x-5}{x+3} \geq 5$

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**February Regional****Algebra II Team Question 14**

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Given that  $2x^2 - 7x + 9$  is the dividend,  $2x - 3$  is the quotient, and the remainder is 3, find the divisor,  $A(x)$ .

Let  $B$  be the remainder when  $x^8 - 3x^5 + 4x^4 + 3x^3 + 2x - 1$  is divided by  $x + 1$ .

When  $\frac{x^3 + (k-1)x + 3}{x+1}$  has remainder 5,  $C$  is the value of  $k$ .

Evaluate the function  $A(x)$ , where  $x = B + C$ .

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When  $\frac{x^3 + (k-1)x + 3}{x+1}$  has remainder 5,  $C$  is the value of  $k$ .

Evaluate the function  $A(x)$ , where  $x = B + C$ .

Let  $A$  be the largest of 3 consecutive odd integers whose sum is 51.

Let  $B$  be the smallest angle of a triangle whose angles are in a ratio of 2:3:4.

Let  $C$  be a two-digit number such that the sum of its digits is 9 and if 9 is added to the number, the digits are reversed.

Find  $(A + B) - C$ .

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Let  $B$  be the smallest angle of a triangle whose angles are in a ratio of 2:3:4.

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Find  $(A + B) - C$ .