

The abbreviation NOTA denotes "None of these answers."

1. Given $f(t) = \sqrt[3]{t}$, $g(t) = \cos t$, $h(t) = (fg)(t)$, and $0 \leq t \leq \pi$ find $h(\pi)$.

- A) $\cos(-1)$ B) -1 C) $\cos\sqrt[3]{\pi}$ D) $-\sqrt[3]{\pi}$ E) NOTA

2. Solve $\frac{x+3}{x} - \frac{2}{x+3} = \frac{6}{x^2+3x}$ over the reals.

- A) $\{-3\}$ B) $\{-3, -1\}$ C) $\{-1\}$ D) $\{1, 3\}$ E) NOTA

3. What is the y -intercept of the graph of $f(x) = b^x$ for real numbers b and x , for positive constant b ?

- A) 0 B) 1 C) b D) $|x|$ E) NOTA

4. Suppose $f(x) = Q + R \ln x$ where Q and R are real constants. If $f(1) = 5$ and $f(e) = 4$, find $\frac{Q}{R}$.

- A) -5 B) $\frac{1}{5}$ C) 4 D) $\frac{1}{4}$ E) NOTA

5. Let (a, b) and (c, d) represent the endpoints of the latus rectum of $x^2 - 6x - 4y + 17 = 0$. Find the sum of the ordinates of these endpoints.

- A) -4 B) -2 C) 4 D) 6 E) NOTA

6. Solve the inequality $\frac{2}{x+3} \leq \frac{1}{x-1}$ $\{x : x \in \square\}$

- A) $(-\infty, -3) \cup (1, 5]$ B) $(-\infty, 5]$ C) $[5, \infty)$ D) $(-3, 1) \cup [5, \infty)$ E) NOTA

7. In right triangle ABC with right angle B , angle $C = 39^\circ$ and side $a = 23$, find side b to the nearest tenth.

- A) 14.5 B) 17.9 C) 28.4 D) 36.5 E) NOTA

8. What is the period of the function $f(t) = \sin^2 t - \cos^2 t$.

- A) $\frac{\pi}{2}$ B) 2 C) π D) 2π E) NOTA

9. Find an equation in terms of x and y whose graph includes the graph of: $x = t^2$, $y = 2t + 1$ for any t .

- A) $4x = (y-1)^2$ B) $4x = (y+1)^2$ C) $4y = (x-1)^2$ D) $4y = (x+1)^2$ E) NOTA

10. 24 students are on tour of the United Nations Building. 12 students speak Russian, 6 speak German, and 15 speak Spanish. Only one student speaks all three languages. 2 students speak Russian and German, but not Spanish. One student does not speak Russian or Spanish and 6 do not speak Spanish or German. All 24 students speak at least one of the three languages. How many students speak both Russian and Spanish, but not German?

- A) 2 B) 3 C) 6 D) 9 E) NOTA

11. Find the inverse of the coefficient matrix for the system of equations:
$$\begin{matrix} x + 2y = 6 \\ 3x + 4y = 12 \end{matrix}$$

- A) $\begin{bmatrix} -2 & 1 \\ 3 & -1 \\ 2 & -2 \end{bmatrix}$ B) $\begin{bmatrix} -\frac{1}{2} & -\frac{3}{2} \\ -1 & -\frac{1}{2} \end{bmatrix}$ C) $\begin{bmatrix} 1 & -\frac{3}{2} \\ -1 & 2 \end{bmatrix}$ D) $\begin{bmatrix} -2 & 1 \\ -3 & \frac{1}{2} \\ 2 & 2 \end{bmatrix}$ E) NOTA

12. Which of the following is equivalent to the expression $\log_f(g+h)$, where f , g , and h are all real numbers greater than 1?

- A) $f \ln(h+g)$ B) $f \ln h \ln g$ C) $\ln \frac{h+g}{f}$ D) $\frac{\ln(h+g)}{\ln f}$ E) NOTA

13. Solve for x : $y = 1 + \frac{1}{1 + \frac{1}{x}}$

- A) $x = 1 - \frac{1}{y}$ B) $x = \frac{y-1}{y}$ C) $x = \frac{1-y}{y-2}$ D) $x = \frac{y+1}{2+y}$ E) NOTA

14. Find the perimeter (to the nearest tenth) of a 45° slice of large circular cheese pizza if the slice is a sector and the pizza has a 14-inch-diameter.

- A) 14.1" B) 19.5" C) 20.3" D) 36.0" E) NOTA

15. The expression $\frac{5x^2 + 7x - 4}{x^3 + 4x^2}$ is equal to $\frac{A}{x} + \frac{B}{x^2} + \frac{C}{x+4}$. Find C .

- A) -1 B) 1 C) 2 D) 3 E) NOTA

16. How many real numbers between 0 and 2π solve the equation $4\cos^2 x - 3 = -\cos x$?

- A) 0 B) 1 C) 2 D) 3 E) NOTA

17. Find all horizontal and vertical asymptotes of $f(x) = \frac{2x-4}{x^2-4}$.

- A) $x = 0, x = 2, y = -2$ B) $x = -2, x = 2, y = 0$
 C) $x = -2, y = 0$ D) $x = 0, y = 2$ E) NOTA

18. Which ordered pair is **not** in the *inverse* of the relation given by $x^2y + y^2 = 10$?

- A) $(1, \sqrt{3})$ B) $(2, -\sqrt{3})$ C) $(1, -3)$ D) $(2, \sqrt{3})$ E) NOTA

19. Given $\sin \theta = 0.4$ and $\cot \theta > 0$, find $\sin(-\theta) + \tan(-\theta) + \csc(\theta)$ to the nearest hundredth.

- A) -3.29 B) -1.76 C) 1.66 D) 2.51 E) NOTA

20. Find twice the product of all the real zeros of the function $g(x) = x^3 + 3x^2 - 16x - 48$.

- A) -64 B) -24 C) 48 D) 96 E) NOTA

21. How many positive real x-coordinates of the solutions exist for the system of equations:
 $y = 2e^{2x} - 3$
 $e^x = -\frac{1}{5}y$?

- A) 0 B) 1 C) 2 D) 3 E) NOTA

22. If $2x^2(x-4)^{\frac{1}{2}} + \frac{x}{2}(x-4)^{\frac{1}{2}}$ is rewritten in the form $\frac{Ax^2 - 4x}{2\sqrt{x-4}}$, find the value of A.

- A) -15 B) -4 C) 2 D) 5 E) NOTA

23. For oblique triangle DEF where E is an obtuse angle, $\sin(D+E)$ is equal to:

- A) $\sin(D+F)$ B) $\sin(E)$ C) $\sin(E+F)$ D) $\sin(F)$ E) NOTA

24. What is the domain of the function $f(x) = \frac{\sqrt{4-x^2}}{x+4}$?

- A) $[-2, 2]$ B) $(-2, 2)$ C) $(-\infty, -2) \cup (2, \infty)$ D) $[0, 2]$ E) NOTA

25. Which is an equation of a sinusoid that passes through the point $(2,0)$, has period $\frac{\pi}{3}$ and amplitude 3?
- A) $y = 3\sin(6x-2)$ B) $y = 3\sin(6x-12)$ C) $y = 6\sin\left(\frac{2}{3}\pi x - \frac{4}{3}\right)$ D) $y = 6\sin\left(\frac{2}{3}x - \frac{2}{3}\right)$ E) NOTA
26. The population of Las Vegas, Nevada in January 2000 was 478,000 and has been increasing at the rate of 6.28% each year. At that rate, in what year will the population be 1 million?
- A) 2002 B) 2007 C) 2012 D) 2034 E) NOTA
27. For triangle JKL with angle $K = 57^\circ$, side $j = 11$ and side $k = 10$, find all possible measures for angle J , to the nearest tenth.
- A) no triangle possible B) 92.3° C) 124.3° and 55.7° D) 112.7° and 67.3° E) NOTA
28. State the range of $h(\theta) = \tan \theta \cos \theta$.
- A) $(-\infty, \infty)$ B) $[-\pi, \pi]$ C) $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$ D) $(-1, 1)$ E) NOTA
29. If the area of a triangle with sides 7, 8, and 9 equals $a\sqrt{b}$ in simplified radical form, find ab .
- A) 30 B) 60 C) 84 D) 504 E) NOTA
30. Find the acute angle θ that satisfies $\cot \theta = \frac{4}{\sqrt{48}}$
- A) $\frac{\pi}{3}$ B) $\frac{\pi}{4}$ C) $\frac{\pi}{5}$ D) $\frac{\pi}{6}$ E) NOTA