

1. Let  $f(x) = \frac{x-1}{x+2}$  and  $g(x) = \sqrt{9-x^2}$  and  $h(x) = e^{x+2}$ .

$A$  = the value of the least integer in the domain of  $g$ .

$B$ : The horizontal asymptote of the graph of  $f$  has equation  $y = B$ .

$C$  = the value of  $f\left(f\left(\frac{1}{2}\right)\right)$ .

$D$  = the real value of  $x$  for which  $h(x) = 1$ .

Give the value of  $A \cdot B \cdot C \cdot D$ .

2.  $S = \{\sqrt{\pi^2}, \sqrt[3]{0.8}, \sqrt[3]{-1}, \sqrt{(0.16)^{-1}}\}$        $T = \left\{1, 3, 5, \frac{-1}{7}\right\}$

Consider the sets  $S$  and  $T$  above, each with four members.  $[x]$  is defined as the greatest integer less than or equal to  $x$ .

$A$  is the least RATIONAL member of set  $S$ .

$B$  is the least value of  $[x]$  for  $x$  a member of set  $T$ .

$C$  is the sum of the positive prime (integer) members of both sets.

$D$  is the greatest value of  $[x]$  for  $x$  a member of either set.

Give the value of  $A + B + C + D$ .

3.  $A$ :  $3 + \sqrt{3} + \frac{1}{3 + \sqrt{3}} + \frac{1}{\sqrt{3} - 3} = x + y\sqrt{z}$  for  $z$  a prime number. Let  $A = x \cdot y \cdot z$ .

$B$ : If the edge of a cube is increased by 50% then the surface area of the cube is increased by  $B\%$ .

$C$  = The least positive value of  $\theta$  for which the graph of  $r = 3\sin(2\theta)$  has maximum radius ( $r$ ).

$D = \ln\left(\tan\left(\frac{\pi}{4}\right)\right) + \cos^{-1}\left(-\frac{1}{2}\right)$ .

Give the value of  $A + B + \frac{12 \cdot C \cdot D}{\pi^2}$ .

4.  $A = \left(\cos\frac{\pi}{3} + i\sin\frac{\pi}{3}\right)^2$        $B = \frac{1}{i^{101}}$

$C$  = the real zero of the function  $f(x) = x^3 - 2x^2 + x - 2$ .

$D$  = the rational value of  $p$  if the function  $g(x) = x^3 - qx^2 - 4x + p$  has zeros (roots) which

include  $\sqrt{7} + 1$  and 1.  $q$  and  $p$  both are rational constants. Give the value of  $\frac{A \cdot C \cdot D}{B}$ .

$$5. \quad f(x) = \frac{1}{8}(x+2)^2 + 3 \quad g(x) = \frac{\sqrt{36-4x^2}}{3} \quad h(x) = \ln|x-1|$$

$A$  = the sum of the coordinates of the focus of the graph of  $f$ .

$B$  = the maximum  $y$ -value of the graph of  $g$ .

$C$  = the value of  $k$  for which  $h(17) = k \cdot \ln(2)$ .

$D$  = the positive value of  $x$  for which  $g(x) = \frac{2}{3}$ .

Give the value of  $A \cdot B \cdot C \cdot D$ .

6. In  $\triangle RST$ ,  $RS = 5$  and  $RT = 6$ .

A: If the area of  $\triangle RST$  is  $\frac{15}{2}$  and  $\angle R$  is acute, then  $m\angle R = A$  radians.

B: If  $ST = 4$  then  $B$  is the value of  $\cos R$ .

C: If  $m\angle T = 30^\circ$  and  $\triangle RST$  is acute then  $\cos S = C$ .

D: If the perimeter of  $\triangle RST$  is 18 then  $D$  is the area of  $\triangle RST$ .

Give the value of  $5 \cdot A \cdot B \cdot C \cdot D$ .

$$7. \quad A = \frac{1}{4}\sqrt{2} + \frac{1}{16}\sqrt{2} + \frac{1}{64}\sqrt{2} + \dots$$

$B$  = the value of  $(x-y)$  when  $4^{3x+y} = \frac{1}{16}$  and  $3^{x+y} = \frac{1}{81}$ .

$C$  = the positive value of  $k$  to make  $x^2 - 2kx + 12$  have one real root of multiplicity 2.

$D$  = the coefficient of the 3<sup>rd</sup> term of the expansion of  $(x-2y)^5$ .

Give the value of  $A \cdot B \cdot C \cdot D$ .

$$8. \quad f(x) = x^2 - 1 \quad g(x) = x^2 + 2x \quad h(x) = x + 1$$

$A$  = the least value of  $k$  so that  $g(h(k)) = 35$ .

$B$  = the real value of  $p$  so that  $\log(f(p)) - \log(h(p)) = 1$ .

$C$  = the value of  $m$  so that  $f(m) - g(m) = \frac{1}{3} \cdot h(m)$ .

$D$  = the sum of the real values of  $n$  so that  $\sqrt{g(n)+1} = 4$ .

Give the value of  $A + B + 7C + D$ .

9. A function is defined parametrically by  $x(t) = 2 - t$  and  $y(t) = \frac{1}{4+t}$ .

$A$  = the  $y$ -intercept of the graph of the function on the  $xy$ -plane.

$$B = \lim_{t \rightarrow \infty} y(t)$$

$C$  = the product of the  $x$ - and  $y$ -coordinates of the function when  $y(t) = -\frac{1}{6}$ .

$D$  = the value of  $k$  such that the equation  $x = k$  is an asymptote of the graph of the function on the  $xy$ -plane.

Give the value of  $B + (A \cdot C \cdot D)$ .

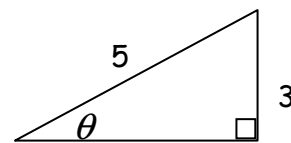
10.  $A = \cos(2\theta)$

$$B = \sin\left(\theta + \frac{\pi}{2}\right)$$

$$C = \sin(\pi - \theta)$$

$$D = \cos(-\theta)$$

Give the value of  $(5A) + B + C + D$ .



Use the triangle above and acute angle  $\theta$  as shown for question #10.

11.  $i = \sqrt{-1}$ .  $A + Bi$  is the value of  $\left(\cos \frac{\pi}{3} + i \sin \frac{\pi}{3}\right)^4$ .

$C + Di$  is the solution of the equation  $x^3 = i$ , where  $C > 0$ ,  $D > 0$ .

Give the value of  $A + B + C + D$ .

12. The completely factored form of  $x^6 - 1$  has two binomial factors and two trinomial factors.  $A$  = the sum of the constant terms of each of these four polynomial factors.

Find  $B$  and  $C$  such that  $\sqrt{B} + \sqrt{C} = \sqrt{3 + \sqrt{8}}$ , so  $B > C$  and  $B$  and  $C$  are rational constants.

Find  $D$  such that  $\frac{1}{D-1} + \frac{1}{D+1} = -\frac{4}{3}$  and  $D > 0$ .

Give the value of  $A \cdot B \cdot C \cdot D$ .

13. 31 students were surveyed about courses they were taking in college.

10 students were taking Advanced Algebra. 12 students were taking Chemistry. 15 students were taking Biology.

5 students were taking Advanced Algebra and Chemistry. 1 student was taking Biology and Advanced Algebra. 2 students were taking Chemistry and Biology. 1 student took all three courses.

Let  $R$  be the number of students who took Advanced Algebra but not Chemistry and not Biology.

Let  $S$  be the number of students who took Chemistry and Biology but not Advanced Algebra.

Let  $T$  be the number of students who took none of these three courses.

Give the value of  $R \cdot S \cdot T$ .

14. John ate  $\frac{1}{2}$  of a pile of M&Ms®. Mary ate  $\frac{1}{4}$  of the remaining M&Ms®.

$A$  = the number of M&Ms® in the original pile (before John ate some) if there were 21 M&Ms® left after Mary ate her share.

$B$  = the percent of M&Ms® that Mary ate, of the original pile (before John ate some).

$C$  = the percent of decrease of the number of M&Ms® from the original pile to the pile that Mary left, if there were 21 M&Ms® in the original pile.

Give the value of  $A + B + C$ .

15.

Consider the polar graphs  $P: r = 4 \cos \theta$ ,  $Q: r = 6$ , and  $S: r = 3 - 4 \cos \theta$ .

$A$  = the area of the graph  $P$ .

$B$  = the area of the graph  $Q$ .

$C$  = the  $y$ -coordinate of the point, in rectangular form, on the curve of  $S$  when  $\theta = -\frac{\pi}{2}$ .

$D$  = the minimum  $x$ -coordinate of graph  $S$ , when graphed on the  $xy$ -plane.

Give the value of  $A + B + C \cdot D$ .