

1. $2-i$ A: Multiplying the three numbers, we get $(-i)(i)(1) = -i^2 = 1$

B: Multiplying both top and bottom by the conjugate of the bottom, we get $\frac{(1+i)^6}{(2)^3} = \frac{-8i}{8} = -i$

C: Since the imaginary parts always cancel out, the sum of the roots is still -2 .

D: Factoring the sum of cubes, we get $x^3 + 27 = (x+3)(x^2 - 3x + 9)$. Therefore, the product of the imaginary roots is 9.

Thus, $1-i-8+9 = 2-i$.

2. **-4** To find the equation of the reflected line, we just need a reflected point and the intersection. The intersection is $(2,0)$. A random point on line B is $(4,3)$. The line that runs through this point and runs perpendicular to A is $y-3 = -2(x-4) \Rightarrow y = -2x+11$ and intersects A at the point $(\frac{24}{5}, \frac{7}{5})$. The reflected point must be the same x and y distances from the intersection,

or $(\frac{24}{5} + \frac{24}{5} - 4, \frac{7}{5} + \frac{7}{5} - 3) = (\frac{28}{5}, -\frac{1}{5})$. The slope of the reflected line is $\frac{0 + \frac{1}{5}}{2 - \frac{28}{5}} = -\frac{1}{18}$ and the line

is $y = -\frac{1}{18}(x-2) = -\frac{x}{18} + \frac{1}{9}$. Thus, $\frac{FB}{K} = \frac{2(\frac{1}{9})}{-\frac{1}{18}} = -4$.

3. **94** A: The determinant of the inverse is the reciprocal of the determinant of the original matrix. $-\frac{1}{21}$

B: For a diagonal, upper triangular, or lower triangular matrix, the determinant is equal to the product of the elements in the diagonal. 120

C: 1

D: First replace each element by its minor to get $\begin{bmatrix} -16 & -1 & 12 \\ -1 & -4 & 6 \\ -4 & 5 & 3 \end{bmatrix}$. Next, switch the sign on every other

element to get $\begin{bmatrix} -16 & 1 & 12 \\ 1 & -4 & -6 \\ -4 & -5 & 3 \end{bmatrix}$. The next step is to transpose the matrix: $\begin{bmatrix} -16 & 1 & -4 \\ 1 & -4 & -5 \\ 12 & -6 & 3 \end{bmatrix}$. The final

step is to multiply by the reciprocal of the determinant, but we can sum the terms first, so $\frac{-18}{-21} = \frac{6}{7}$

$-21+120+1-6 = 94$

4. $\frac{7}{170}$ A: Through binomial probability, we see that

$$P(Y \leq 3) = \left(\frac{1}{2}\right)^7 (7C0 + 7C1 + 7C2 + 7C3) = \frac{1}{2}.$$

B: The setup is as follows: $n(n-1) = \frac{n(n-1)(n-2)}{6} \Rightarrow n-2 = 6 \Rightarrow n = 8.$

C: For the condition to be satisfied, the permutation must have the following form:

XXXXX, where the are places for the vowels to go and the X's are places for the consonants.

There are 5 slots for the first vowel, 4 for the next, and 3 for the one after, so there are 120 ways to

arrange the vowels, and $4! = 24$ ways to arrange the consonants, for a probability of $\frac{(4!)(60)}{7!} = \frac{2}{7}.$

$$\left(\frac{1}{2}\right)\left(\frac{12}{85}\right)\left(\frac{7}{2}\right) = \frac{21}{85}.$$

D: Factoring 180, we see that the prime factorization is $180 = 2^2 \cdot 3^2 \cdot 5$, so there are $(3)(3)(2) = 18$ positive integral factors. A number is even if it is divisible by two, so we can see that there are $3(2) = 6$ factors of 180 that are comprised of only 3's and 5's. Therefore, the probability that a chosen factor is even

is $1 - \frac{1}{3} = \frac{2}{3}.$

The final answer is $\frac{7}{170}$

5. **438** A: Completing the square, we can put the equation in vertex form, or $(y-1)^2 = x-2$, so the length of the latus rectum is $4p = 1.$

B: Completing the square, we rearrange the equation to be $\frac{(x-1)^2}{6} + \frac{(y+2)^2}{18} = 1$, which tells us

that $a = 3\sqrt{2}, b = \sqrt{6}, c = 2\sqrt{3}$. Therefore, $c^2 = 12.$

C: Rearrange the equation to get $(x+2)^2 - (y-3)^2 = 7$, so the sum of the coordinates of the center is 1.

D: Plugging in $y = 2x$ into the circle, we get $5x^2 - 15x + 10 = 0$, so the product of the x-coordinates of the intersection is 2. Since every y value is twice the x value ($y = 2x$), the product of the y values should be 4 times the product of the x values. Thus, the product of all coordinates is 16.

The final answer is $A + 3B^2 + C + 25D = 1 + 36 + 1 + 400 = 438.$

6. **1341** A: If we let $S = 1(2) + 2(2^2) + 3(2^3) + \dots + 6(2^6)$
 $2S = 2^2 + 2(2^3) + 3(2^4) + \dots + 6(2^7)$, then $S - 2S = -S = 2 + 2^2 + 2^3 + \dots + 2^6 - 6(2^7),$

or $-S = \frac{2 - 2(2^6)}{1 - 2} - 6(2^7) = 642$

B: This is just an infinite geometric series, which has a sum $\frac{1}{1 - \frac{2}{3}} = 3.$

C: The first few terms are as follows: $\{a_0, a_1, a_2, a_3 \dots a_{15}\} = \{1, 1+1, 1+1+2, \dots, 1+1+2+\dots+15\}$, so it's clear that each number is one more than a triangular number. The sum of the first 20 triangular numbers is $\frac{n(n+1)(n+2)}{6} = \frac{15(16)(17)}{6} = 680$. Adding 16 to this number gives us 696.

Thus, $A + B + C = 696 + 642 + 3 = 1341$

7. $[3, \infty)$ The domain of the functions are A: $(-\infty - 2) \cup (-1, \infty)$, B: $(2, \infty)$, C: $(-\infty - 1) \cup (1, \infty)$, D: $[3, \infty)$. The intersection of these domains is $[3, \infty)$.

8. **84** We see that $f(1+1) = f(1) + f(1) + 1 + 1 \Rightarrow f(2) = 8$ and $f(3) = f(2) + f(1) + 1 + 2 = 14$. There are two different values of $f(4)$, namely $f(4) = f(3) + f(1) + 3 + 1 = 21$ and $f(4) = f(2) + f(2) + 2 + 2 = 20$. There are three different values of $f(5)$,

$$f(5) = f(2) + f(3) + 2 + 3 = 27$$

$f(5) = f(1) + f_1(4) + 1 + 4 = 29$. Doing the same operations, we see the values of $f(6)$ are

$$f(5) = f(1) + f_2(4) + 1 + 4 = 28$$

The sum of these values is $\frac{3}{2}(27 + 29) = 84$.

9. **7** The asymptotes are as follows: a) $x = 0$, b) $y = 5$, c) $y = 1, x = 1$, d) $y = 1, x = 4$, e) None f) $y = 2, x = -3$ The number of distinct asymptotes is 7.

10. **12 A:** Working off the distance = rate X time formula, we get $1 = \frac{3}{2} \left(\frac{1}{2} + \frac{1}{J} \right) \Rightarrow J = 6$.

B: Same formula, $1 = 1 \left(\frac{1}{2} + \frac{1}{6} + \frac{1}{R} \right) \Rightarrow R = 3$.

C: Same formula, $1 = \frac{3}{4} \left(\frac{1}{2} + \frac{1}{6} + \frac{1}{3} + \frac{1}{M} \right) \Rightarrow M = 3$

The sum is **12**.

11. $78 - 4\sqrt{5}$ A: The sum is $-\frac{b}{a} = -2$.

B: We see that $(a+b)^2 - 4ab = a^2 - 2ab + b^2 = (a-b)^2$. Therefore, $a-b = \sqrt{4-4(-4)} = 2\sqrt{5}$. We also know that $a^2 - b^2 = (a+b)(a-b) = -2(2\sqrt{5}) = -4\sqrt{5}$.

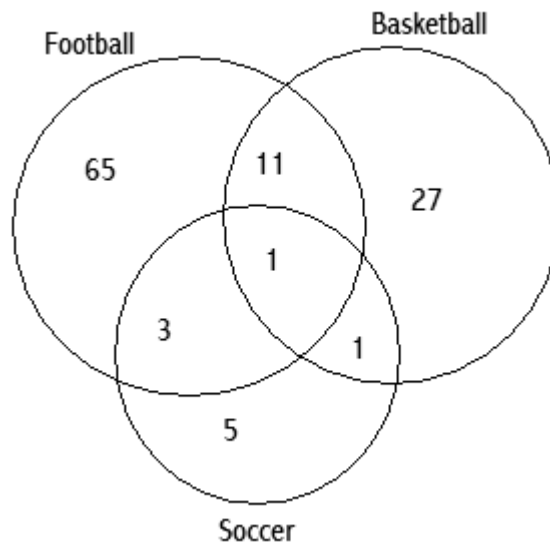
C: We can see that $(a+b)^2 - 2ab = a^2 + b^2$, so $a^2 + b^2 = 4 - 2(-3) = 10$. Also,

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2) = -2(12 + 4) = -32.$$

D: Our answer is $a^4 + b^4 = (a^2 - b^2)^2 + 2a^2b^2 = 80 + 2(-4)^2 = 112$

The sum is $78 - 4\sqrt{5}$.

12. **124** Refer to the accompanying Venn diagram.
 A: The sum of the elements in the diagram is 113, so 7 are not fans of any of the three sports.
 B: 5 of the soccer fans are fans of either football or basketball.
 C: 15 students are fans of exactly 2 sports.
 D: The number of students that satisfy this condition is $65 + 27 + 5 = 97$



13. $\frac{1}{8}$ Putting the parabola in vertex form gives
 us $y = (x + 1)^2$, so the length of the latus rectum is 1,
 and $p = \frac{1}{4}$, so the area is $A = \frac{1}{2} \cdot \frac{1}{4} \cdot 1 = \frac{1}{8}$.
14. $-\frac{1}{2}$ The inverse functions are $f^{-1}(x) = \frac{x}{2} + \frac{1}{2}$ and $g^{-1}(x) = x + 2$. Plugging in all the values, we
 get $-\frac{1}{2}$ as the final answer.
15. $2\sqrt{10}$ Since the snake is only 10 units long, we only need to worry about the last ten units traveled.
 Thus, vertical distance between head and tail is 6 and the horizontal distance is 2. Total distance
 is $\sqrt{36 + 4} = 2\sqrt{10}$.