

**FAMAT 2004 STATE CONVENTION
THETA INDIVIDUAL
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1) Distributive Property → **D**

2) $m\angle ABC + m\angle BCA = 105$

Since $m\angle ABC = 2 \cdot m\angle BCA$, then

$$2 \cdot m\angle BCA + m\angle BCA = 105$$

$$3 \cdot m\angle BCA = 105$$

$$m\angle BCA = 35$$

$$\therefore m\angle ABC = 70 \rightarrow \mathbf{C}$$

3) $P(x) = 2004(x^{2004} + x^{2003} + x^{2002} + x^{2001} + \dots + x^0)$
 $P(-1) = 2004(1 + -1 + 1 + -1 + \dots + 1)$
 $= 2004(1)$
 $= 2004 \rightarrow \mathbf{A}$

4) $\det[A] = (7 \cdot 5) - (-4 \cdot 9) = 71$

$$A^{-1} = \frac{1}{71} \begin{pmatrix} 5 & -9 \\ 4 & 7 \end{pmatrix}$$

$$\text{sum of entries} = \frac{1}{71}(5 + -9 + 4 + 7) = \frac{7}{71} \rightarrow \mathbf{C}$$

5) Can not be done. You can not take the even root of a negative number over the Real numbers → **E**

$$6) \frac{r^2 - s^2}{2s^2 - rs - r^2} \cdot \frac{r^2 - 4s^2}{s^2 + rs - 2r^2} = \frac{-1(r+s)(s-r)}{(2s+r)(s-r)} \cdot \frac{(r+2s)(r-2s)}{-1(s+2r)(r-s)}$$

$$= \frac{(r+s)(r-2s)}{(2r+s)(r-s)} \rightarrow \mathbf{C}$$

7) Convergent Geometric Series

$$r = \frac{\frac{D}{6}}{\frac{D}{6}} = \frac{1}{6}; \quad S = \frac{t_1}{1-r} = \frac{\frac{D}{6}}{1-\frac{1}{6}} = \frac{D}{5} \rightarrow \mathbf{A}$$

$$8) \begin{pmatrix} (6 \cdot -2) + (3 \cdot 1) & (6 \cdot -3) + (3 \cdot 4) \\ (-4 \cdot -2) + (5 \cdot 1) & (-4 \cdot -3) + (5 \cdot 4) \\ (2 \cdot -2) + (-1 \cdot 1) & (2 \cdot -3) + (-1 \cdot 4) \end{pmatrix}$$

$$= \begin{pmatrix} -9 & -6 \\ 13 & 32 \\ -5 & -10 \end{pmatrix} \rightarrow \mathbf{C}$$

9) Area = $(28)(12)(\pi) \approx 1055.6 \text{ ft.}^2$
 $1055.6 \div 200 \approx 5.3$ gallons
 Will need to buy 6 gallons → **C**

10) Exponential decay.
 Value = $(23000)(0.82)^8$
 $= \$4701.52 \rightarrow \mathbf{B}$

11) Vertex is at $(0, -2)$. Point on parabola is $(-4, 2)$.
 $x = a(y - k)^2 + h \rightarrow -4 = a(2 + 2)^2 + 0$
 $-4 = 16a$

$$\frac{-1}{4} = a$$

Sun is at the focus. $\frac{-1}{4} = \frac{1}{4m} \rightarrow m = -1$

$(-1, -2) \rightarrow \mathbf{D}$

12) $4.4 + (-6.3) - (-8.1) = 6.2$

$$\sqrt[5]{7^{6.2}} = 7^{\frac{6.2}{5}} = 7^{1.24} \rightarrow \mathbf{B}$$

13) $SA = 2\pi rh + 2\pi r^2$
 $= 2\pi(2)(6) + 2\pi(2)^2$
 $= 24\pi + 8\pi$
 $= 32\pi \rightarrow \mathbf{C}$

14) $\frac{3x+16}{(x-3)(x+2)} = \frac{A}{x-3} + \frac{B}{x+2}$
 $3x+16 = A(x+2) + B(x-3)$
 let $x = -2 \rightarrow 10 = -5B$
 $-2 = B$
 let $x = 3 \rightarrow 25 = 5A$
 $5 = A$
 $-2 + 5 = 3 \rightarrow \mathbf{A}$

15) $(\sqrt{35+14\sqrt{6}})^2 = (\sqrt{x} + \sqrt{y})^2$
 $35 + 14\sqrt{6} = x + 2\sqrt{xy} + y$
 $35 = x + y$
 $14\sqrt{6} = 2\sqrt{xy}$
 $(7\sqrt{6})^2 = (\sqrt{xy})^2$
 $294 = xy$
 $\therefore 21, 14$
 $|21-14| = 7 \rightarrow \mathbf{C}$

16) $\frac{1}{\sqrt[3]{4} + \sqrt[3]{10} + \sqrt[3]{25}} \cdot \frac{\sqrt[3]{2} - \sqrt[3]{5}}{\sqrt[3]{2} - \sqrt[3]{5}} = \frac{\sqrt[3]{2} - \sqrt[3]{5}}{2-5}$
 $= \frac{\sqrt[3]{2} - \sqrt[3]{5}}{-3}$
 $= \frac{\sqrt[3]{5} - \sqrt[3]{2}}{3} \rightarrow \mathbf{D}$

17) **C**

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- 18) $75 + 50 = 125$. Discounts are taken separately.
 $125 \bullet 0.4 = 50 \rightarrow 125 - 50 = 75$
 $75 \bullet 0.2 = 15 \rightarrow 75 - 15 = 60$
 $60 \bullet 0.06 = 3.6$
 $60 + 3.6 = \$63.60 \rightarrow \mathbf{C}$

- 19) Paul mowed $\frac{1}{4}$ of the lawn in one hour, so his rate is

$\frac{1}{4}$ or 0.25. $\frac{3}{4}$ or 0.75 of the lawn remains. Let $g =$

Greg's rate. 1 hour, 48 minutes = 1.8 hours.

$$\begin{aligned} (g)(1.8) + (0.25)(1.8) &= 0.75 \\ 1.8g + 0.45 &= 0.75 \\ 1.8g &= 0.3 \end{aligned}$$

$$g = 0.1666\dots \text{ or } \frac{1}{6}$$

So, Greg can mow the lawn in 6 hours alone $\rightarrow \mathbf{A}$

- 20) ${}_{15}C_6(3x^2)^9 \left(\frac{-2}{3}\right)^6 = (5005)(19683)(64) =$
 $6304858560 \rightarrow \mathbf{D}$

- 21) $F = \frac{9}{5}C + 32$
 $= \frac{9}{5}(30) + 32$
 $= 86 \rightarrow \mathbf{C}$

- 22) $P(\text{exactly 1 will be in an accident}) = \frac{25000}{500000} = 0.05$

$$P(1 \text{ will not be in an accident}) = 1 - 0.05 = 0.95$$

$$P(2 \text{ of 3 will be in an accident}) =$$

$${}_{3}C_2(0.05)^2(0.95)^1 = 0.007125 \rightarrow \mathbf{C}$$

- 23) Geometric Means. $82 = 39 \bullet r^{6-1}$

$$\frac{82}{39} = r^5 \rightarrow r \approx 1.160245383$$

$$R = 39(1.160245383) = 45.2496$$

$$S = 39(1.160245383)^2 = 52.5006$$

$$T = 39(1.160245383)^3 = 60.9136$$

$$V = 39(1.160245383)^4 = 70.6747$$

$$R+S+T+V \approx 229 \rightarrow \mathbf{A}$$

- 24) determinant = $x^3 - 3x + 2$

$$x^3 - 3x + 2 = 0$$

$$(x-1)(x^2 + 2x - 2) = 0$$

$$(x-1)(x+2)(x-1) = 0$$

$$x = 1, -2, 1$$

$$1 + (-2) + 1 = 0 \rightarrow \mathbf{C}$$

- 25) $y = \log_5 x$
 $x = \log_5 y$
 $y = 5^x$
 $g^{-1}(x) = 5^x \rightarrow \mathbf{A}$

- 26) Similar triangles.

$$\frac{TN}{TG} = \frac{TR}{TG} \rightarrow \frac{2}{TG} = \frac{2}{6}$$

$$(TG)^2 = 12$$

$$TG = \sqrt{12}$$

$$= 2\sqrt{3} \rightarrow \mathbf{B}$$

- 27) $\log_6 36 = 2$; $\log_1 \frac{1}{8} = 3$; $\log_3 \frac{3}{\sqrt{3}} = \frac{1}{2}$; $\log_4 2 = \frac{1}{2}$;

$$2 + 3 + \frac{1}{2} + \frac{1}{2} = 6 \rightarrow \mathbf{C}$$

- 28) The units digit is periodic every 4 times.

$$3^0 = 1 \qquad 3^4 = 1$$

$$3^1 = 3 \qquad 3^5 = 3$$

$$3^2 = 9 \qquad 3^6 = 9$$

$$3^3 = 7 \qquad 3^7 = 7$$

$2004 \div 4$ has a remainder of 0, so the units digit is 1 $\rightarrow \mathbf{A}$

- 29) $(0.43)(60) + 0.8x = 0.6(60 + x)$

$$25.8 + 0.8x = 36 + 0.6x$$

$$0.2x = 10.2$$

$$x = 51 \rightarrow \mathbf{B}$$

- 30) $P(-x) = 6x^7 - 2x^6 - 3x^5 + 2x^4 + 7x^3 + x^2 + 9x - k$
 3 sign changes $\rightarrow \mathbf{C}$