

Algebra II Team Answers: January Regional

Let's '99

1. -39

2. 3

3. 11.3 (or  $11\frac{3}{10}$  or  $\frac{113}{10}$ )

4. 18

5.  $\frac{4}{21}$  (question specified "fraction form")

6.  $\frac{2\sqrt{5}+1}{19}$  (or  $\frac{2\sqrt{5}}{19} + \frac{1}{19}$ )

7. 16

8. 29

9. 2

10. 189.51 (question specified "hundredths place")

11. 57

12. 13

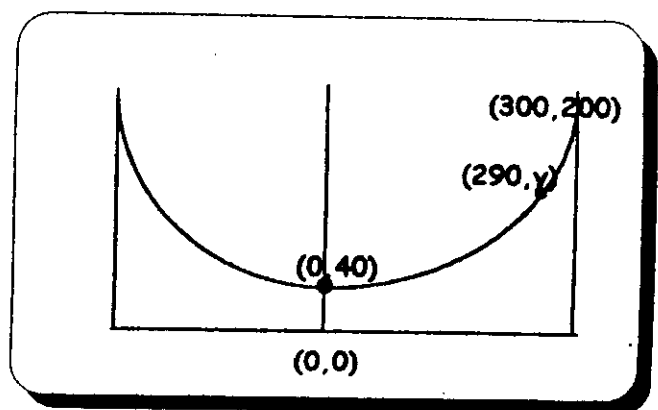
13. 6.25 (or  $6\frac{1}{4}$  or  $\frac{25}{4}$ )

14. \$273 (dollar sign not necessary)

15. 97.9 (or  $\frac{979}{10}$  or  $97\frac{9}{10}$ )

Answers/Solutions: Algebra II, Team Questions. January Regional

- $x = -16$ ,  $yz = 3^{\frac{4}{3}} \cdot 3^{\frac{1}{3}} = 3^{\frac{5}{3}} = 3\sqrt[3]{9}$  so  $xyz = -48\sqrt[3]{9}$ . Therefore  $a+b=(-48)+9=-39$
- $k = \frac{1}{2}$  for  $f(x)$  and for  $f(x-1)$ , the x-intercept is  $\frac{3}{2}$ .  $\frac{1}{2}c = \frac{3}{2}$  when  $c = 3$ .
- $[8(k+1) + -30 + 216] - [-32 + 90 + 18(k+1)] = 5$ . The value of  $k = \underline{11.3}$
- Multiplying the equation by the common denominator:  $(x+2)(x+3) + 2(x)(x+3) = 5x(x+2)$   
 $x^2 + 5x + 6 + 2x^2 + 6x = 5x^2 + 10x$  and  $2x^2 - 1x - 6 = 0$ . Adding 18 to both sides of the equation,  $2x^2 - 1x + 12 = 18$ . The answer is 18.
- The sum of the roots of the function is  $-\frac{b}{a}$ . So the sum of the roots is  $61/4$ . Subtracting 11, the sum of the remaining roots is  $4.25 = k$ .  $K+1=5.25$  and the reciprocal of  $5\frac{1}{4}$  is  $\frac{4}{21}$ .
- $6^x \cdot 7^x = c^2$  so  $(4)(5) = c^2$ .  $c = \sqrt{20} = 2\sqrt{5}$ .  $\frac{1}{2\sqrt{5}-1} = \frac{2\sqrt{5}+1}{19}$  (use the conjugate)
- $\log_3 m = 16$  so  $3^{16} = m$ . Using the sequential counting principle,  $m$  can have a factor of  $3^0, 3^1, \dots, 3^{16}$  or 17 factors. So  $A=17$ . In the second equation,  $x=1$  so  $y=0$  and  $(2x)^0 = 1$  so  $B=1$  and  $A-B = 17-1 = \underline{16}$ .
- $\frac{200+x}{254+x} = 0.795$  and  $x = 9.41$  so  $P=10$  games. Note that at 9 games, the computer will compute the percentage at less than 80%. For the second question,  $\frac{200+0.90x}{254+x} = 0.795$  and for that equation,  $x=18.38$  and  $Q=19$ .  $P+Q = \underline{29}$ .
- $\frac{A}{x+3} + \frac{B}{x+4} = \frac{1}{(x+3)(x+4)}$  gives  $Ax + 4A + Bx + 3B = 1$  (obtaining a common denominator and setting numerators equal). So  $A+B = 0$  (the coefficients of the  $x$  term) and  $4A+3B=1$  (the constants). Solving, we get  $A=1$  and  $B = -1$ , so  $A-B = \underline{2}$ .
- $y - 40 = a(x - 0)^2$   
 $200 - 40 = a(300)^2$  from the point  $(300, 200)$ .  
 $a = \frac{2}{1125}$ . Using the point  $(290, y)$  to find the point 10 feet away from the support pole, we get  $y = \underline{189.51}$



11.  $f(2) = f(-2) = 3$  and  $g(5) = 8$  so  $g(-5) = -8$ . (These are by the definitions of even and odd functions.)  $3^2 - 2(3)(-8) = 9 + 48 = 57$ .
12.  $\log(3 \cdot 10) = \log 10 + \log 3 = 1 + y$ .  $\log(4 \cdot 27) = \log(9k)$  so  $k = 12$ , and  $B = 12$ .  
 $C = \frac{\log 3}{\log 2} \cdot \frac{\log 2}{\log 10} = y$ .  $A + B - C = 1 + y + 12 - y = \underline{13}$ .
13. The vertex of the parabola is midpoint between the line  $x = 5$  and the focus  $(7, -1)$  which gives the equation  $\frac{1}{4}(y + 1)^2 = x - 6$ . The  $\frac{1}{4}$  is determined by setting the distance from Focus to Vertex (1) equal to  $\frac{1}{4a}$ . At  $y = 0$ , the  $x$  coordinate is 6.25.
14.  $120 + 5D = 180 + 3D$  gives the "breakeven point" of 30 days. At day 31, when heater B will cost less than heater A, the cost of heater B will be \$273.
15.  $f^{-1}(x) = \frac{x-6}{2}$  and  $f^{-1}(2) = -2$ .  $(f(2))^{-1} = \frac{1}{10}$  and  $g(f(2)) = g(10) = 100$ .  
 $-2 - \frac{1}{10} + 100 = 97.9$