

Algebra I Regional Team Solutions

1.) $2+3+5+7+11+13+17+19+23+29+31+37+41=238$

Answer $238-2=236$

2.) $2^{6y+2} - 2^{6y+3} = \frac{2^{6y+2}}{2^{6y}} - \frac{2^{6y+3}}{2^{6y}} = 2^2 - 2^3 = \text{Answer } -4$

3.) Let $L = \text{length}$ and $W = \text{width}$.
 $L(\frac{4}{5}L) = 2880$
 $L^2 = 3600$
 $L = 60$
 $W = 48$
Answers $48+36$

4.) $-1.2x - .2 [8 - (4-6x)] = .8(x+1)$
 $-1.2x - .2 [8-4+6x] = .8x + .8$
 $-1.2x - .2 [4+6x] = .8x + .8$
 $-1.2x - .8 - 1.2x = .8x + .8$
 $-2.4x - .8 = .8x + .8$
 $-3.2x = 1.6$
 $x = -.5 \text{ or } -\frac{1}{2}$

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5.) $\begin{cases} 3x-17=-4 \\ 8x-y=38 \end{cases} \rightarrow \begin{cases} 3x=4+29 \\ 8x-y=10-38 \end{cases} \rightarrow \begin{cases} 3x=33 \\ 8x-y=-28 \end{cases}$
 $\begin{cases} 3x=33 \\ 8x-y=-28 \end{cases} \rightarrow \begin{cases} x=11 \\ 8(11)-y=-28 \end{cases} \rightarrow \begin{cases} x=11 \\ 88-y=-28 \end{cases} \rightarrow \begin{cases} x=11 \\ -y=-116 \end{cases} \rightarrow \begin{cases} x=11 \\ y=116 \end{cases}$

$3x+y=17$
 $8x-y=38$
 $11x=55$
 $x=5$
 $3(5)+y=17$
 $15+y=17$
 $y=2$
(5, 2)

$3p-2(1)=4$
 $3p-2=4$
 $3p=6$
 $p=2$
(2, 1)

$2a - 5(6) = -1$
 $2a - 30 = -1$
 $2a = 29$
 $a = 14.5$

6.) $b^5 + 36b = 13b^3$
 $b^5 - 13b^3 + 36b = 0$
 $b(b^4 - 13b^2 + 36) = 0$
 $b(b^2 - 9)(b^2 - 4) = 0$
 $b(b-3)(b+3)(b-2)(b+2)$
Answer $0, 3, -3, 2, -2$

7.) $\frac{x}{a} + \frac{y}{b} + \frac{b}{c} = \frac{5}{10} + \frac{2}{2} + \frac{6}{1} = 7\frac{1}{2}$
Answer $7\frac{1}{2}$

$\frac{2A+B}{B-D} = \frac{2(-7)+4}{(-12)-(-12)} = \frac{-10}{0}$
Answer \emptyset

8.) $2 - \frac{2}{3}y - 7 = 3$
 $-\frac{2}{3}y = 8$
 $y = -12$

9.) $2[9+2(9-4)] = 12$
 $2[9+2(5)] = 12$
 $2[9+10] = 12$
 $2[19] = 12$
 $38 = 12$
Answer \emptyset

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8) $\binom{x^2}{3y^3} \cdot \binom{4x^2}{7y^4} \cdot \binom{7y^4}{4x^5} \cdot \binom{3y^3}{2} = \frac{x^2 \cdot 4x^2 \cdot 7y^4 \cdot 3y^3}{3y^3 \cdot 7y^4 \cdot 4x^5 \cdot 2}$

Answer $\frac{9y^2}{20}$

9. Let $x = \#$ of 3 tickets

$y = \#$ of 5 tickets

$3x =$ value of 3 tickets

$5y =$ value of 5 tickets

$$\begin{aligned} 3x &= 3x - 350 \\ 5y &= 5y - 350 \\ 3x + 5y &= 3\left(\frac{4}{3}y\right) - 350 \\ 5y &= 4y - 350 \\ 5y - 4y &= -350 \\ y &= -350 \\ 3x &= 200 \end{aligned}$$

Let $x = 1st$ integer
 $x+1 = 2nd$ integer
 $x+2 = 3rd$ integer
 $x+3 = 4th$ integer
 $3[x+(x+1)] - [x+(x+2)] = 50$
 $3[2x+1] - [2x+5] = 50$
 $6x+3-2x-5=50$
 $4x-2=50$
 $4x=52$
 $x=13$
 Largest integer is $(x+3) = 16$

Answer $A-B = 200 - 16 = 184$

10) Substitute $a = \frac{1}{2}x$ in

$$\begin{aligned} \frac{1}{2}x + 3d &= -6 \\ \frac{1}{2}x + 3\left(\frac{1}{3}x\right) &= -6 \\ \frac{1}{2}x + x &= -6 \\ \frac{3}{2}x &= -6 \\ x &= -4 \end{aligned}$$

(-2) $2c - 1d = -8$
 $4c + 3d = -6$
 $-4c + 2d = 16$
 $5d = 10$

$\frac{1}{2}x = \frac{1}{2}(-4) = -2$
 $a = -2$
 $\frac{1}{2}x + 3d = -6$
 $-2 + 3d = -6$
 $3d = -4$
 $d = -\frac{4}{3}$

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14.) $A = 35^2 - 36^2 = (35+36)(35-36) = (71)(-1) = \boxed{-71}$
 $B = 26^2 - 25^2 = (26+25)(26-25) = (51)(1) = \boxed{51}$
 $C = 45^2 - 43^2 = (45+43)(45-43) = (88)(2) = \boxed{176}$
 $D = 33^2 - 31^2 = (33+31)(33-31) = (64)(2) = \boxed{128}$
 $\frac{a+b+d}{c} = \frac{-71+51+128}{176} = \frac{108}{176} = \frac{27}{44}$
Answer $\frac{27}{44}$

15.) $4 + \frac{1}{4 + \frac{1}{4 + \frac{1}{4 + \frac{1}{4}}}}$
 $\left[4 + \frac{1}{4 + \frac{1}{4} = \frac{17}{4}} \right] = 4 + \frac{1}{\frac{17}{4}} = 4 + \frac{4}{17}$
 $4 + \frac{1}{4 + \frac{1}{4 + \frac{1}{4 + \frac{1}{4}}}} = 4 + \frac{1}{\frac{17}{4}} = 4 + \frac{4}{17}$
 $4 + \frac{1}{\frac{17}{4}} = 4 + \frac{4}{17} = 4 + \frac{72}{305}$
Answer $4 \frac{72}{305}$ or $\frac{1292}{305}$

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11.) A. $(5,6)(-7,9) = \frac{4x-y}{x^2-x} = \frac{9-6}{-7-5} = \frac{3}{-12} = \boxed{-\frac{1}{4}}$
 B. $y = 4x + b$ C. $-2x + y = -8$ D. $xy = 3$
 $(3) = 4(2) + b$ $-2x + (0) = -8$ $y = -1x + 3$
 $3 = 8 + b$ $-2x = -8$ $\frac{\text{Slope} = -1}{\text{Answer}} \boxed{5+1=6}$
 $\boxed{-5=b}$ $\boxed{x=4}$

12.) $\frac{1}{a} + \frac{1}{b} = \frac{2}{3a} + \frac{2}{3b}$
 $\left(\frac{1}{a} + \frac{1}{b} \right) \div \left(\frac{2}{3a} + \frac{2}{3b} \right)$
 $\frac{b+a}{ab} \div \frac{2b+2a}{3ab}$
 $\frac{b+a}{ab} \cdot \frac{3ab}{2(b+a)} = \text{Answer } \boxed{\frac{3}{2}}$

$4^1 = 4$
 $4^2 = 16$
 $4^3 = 64$
 $4^4 = 256$
 $2 \sqrt[4]{48}$ no Remainder
 Thus it must end in 6-Answer
 Remainder 1 would give you a 6.